

HOMework 6:

PREDICATE LOGIC DERIVATIONS

Intro Logic
Ted Sider

1. $\exists x(\sim Fx \& Gx) ; \forall x(Gx \rightarrow Hx) / \text{show } \exists x[\sim Fx \& Hx]$
2. $\forall x(Gx \rightarrow Fx) ; \forall x(Fx \rightarrow [Hx \vee Ix]) ; \forall x(Gx \rightarrow \sim Hx) / \text{show } \forall x(Gx \rightarrow Ix)$
3. $\forall x[(Fx \& Hx) \rightarrow Gx] ; \exists x(Kax \& Jx) ; \exists x Kax \rightarrow \forall x Hx / \text{show } \forall x(Fx \rightarrow Gx)$
4. $\forall x(Lxx \rightarrow Fx) ; \forall x \forall y(Lxy \rightarrow Lxx) ; \forall x \sim Fx / \text{show } \sim \exists x \exists y Lxy$
5. $\forall x(Fx \rightarrow Gx) \vee \forall x(Fx \rightarrow Hx) / \text{show } \forall x(Fx \rightarrow (Gx \vee Hx))$
6. $\exists x \sim Lbx \rightarrow \forall x Lcx ; \forall x(Lcx \rightarrow Lxb) / \text{show } Lba \vee Lab$
7. $\forall x(Fx \rightarrow Gx) ; \forall y[(Fy \& Gy) \rightarrow \sim Hy] ; \sim \forall x \sim Hx / \text{show } \exists x(Hx \& \sim Fx)$
8. $\forall y \exists x Rxy / \text{show } \sim \exists y \forall x \sim Rxy$
9. $\exists y(Gy \& \forall z Ryz) ; \forall y[Fy \rightarrow \exists z \sim Ryz] / \text{show } \exists y(Gy \& \sim Fy)$
10. $\forall x(\forall z Rxz \rightarrow \forall y Ryx) ; \exists z \exists y Ryz ; \forall x \forall y(Rxy \rightarrow \forall z Rxz) / \text{show } \forall z \forall y Ryz$