

# FACT/OPERATOR GROUNDING

Ted Sider  
Ground seminar

## 1. Operator vs predicate

$F_1$  grounds  $F_2$

where ' $F_1$ ' and ' $F_2$ ' are names of facts, versus: =

$\phi$  because  $\psi$

where ' $\phi$ ' and ' $\psi$ ' are replaced by sentences.

In favor of the operator view:

- Neutral about the granularity of facts
- Maintains parallel with operators like 'and' and 'not'
- Keeps the subject matter of ground where it ought to be

But the operator view makes it harder to define notions like “ungrounded”:

- $\sim\exists F'$  ( $F'$  grounds [Snow is white]) *(works fine)*
- $\sim\exists S$ (Snow is white because  $S$ ) *(sentential quantification)*
- $\sim\exists S$ ( $\ulcorner$ Snow is white because  $S$  $\urcorner$  is true) *(what about inexpressible grounds?)*

## 2. Plural arguments

Rather than saying that conjunctions are grounded in *each* of their conjuncts:

$A\wedge B$  because  $A$ , and  $A\wedge B$  because  $B$

we must instead say that they are grounded in the conjuncts *taken together*:

$A\wedge B$  because  $A, B$

**Entailment restated** If  $A$  because  $\Gamma$ , then necessarily: if  $\bigwedge \Gamma$  then  $A$

(“ $\Gamma$ ” takes the place of an arbitrary list of sentences;  $\bigwedge \Gamma$  is the conjunction of those sentences. Note that this definition is a schema.)

### 3. Full versus partial ground

### 4. Some logical issues

**Asymmetry** If  $A$  because  $B, \Gamma$ , then not:  $B$  because  $A, \Delta$

**Irreflexivity** Not:  $A$  because  $A, \Gamma$

**Transitivity** If  $A$  because  $B, \Gamma$  and  $B$  because  $\Delta$ , then:  $A$  because  $\Gamma, \Delta$

**Factivity** If  $A$  because  $\Gamma$ , then  $\bigwedge \Gamma$

**Monotonicity** If  $A$  because  $\Gamma$ , then  $A$  because  $B, \Gamma$

$\wedge$  If  $A$  and  $B$ , then:  $A \wedge B$  because  $A, B$

$\vee$  If  $A$ , then  $A \vee B$  because  $A$

$\exists$  If  $\phi(a)$ , then  $\exists x \phi(x)$  because  $\phi(a)$

Comments:

- Asymmetry implies irreflexivity
- Irreflexivity and hence asymmetry fail for Fine's weak ground
- Transitivity fails for Fine's immediate ground.
- Factivity fails for Fine's nonfactive ground.
- The failure of monotonicity is central to the very idea of ground. The ground is supposed to be relevant to the grounded.
- Fine notes an interesting problem. Given  $\exists, \exists x x=a$  because  $a=a$ ; given Entailment, Necessarily, if  $a=a$  then  $\exists x x=a$ ; since it's necessary that  $a=a$ , it follows that it's necessary that  $\exists x x=a$ ; so  $a$  exists necessarily.

## 5. Is ground fundamental?

What does it mean to say that ground is “primitive”?

**Strongly metaphysically primitive** All facts about ground are fundamental

**Weakly metaphysically primitive** Some facts about ground are fundamental

**Conceptually primitive** ground isn’t defined in terms that don’t involve ground.

**Methodologically** it’s legitimate to talk about ground without having a definition in our pocket.

Argument (from the principle of “purity”) against strong metaphysical primitiveness: it can’t be a fundamental fact that there exists a city because *C*, because no fundamental fact involves cityhood.

If you buy the purity argument, then:

1. *No quick account of connection/levels.* You can still say that different descriptive levels are related by ground, but that isn’t a satisfactory answer to the question of what that relationship consists in.
2. *Ground might yet be modal.* For all the assault on modal *definitions* of ground, ground may yet be grounded in modal terms (or modal plus other stuff).

## 6. Infinite descent

Given path dependent distance, the friend of ground will find herself saying that a certain path is one meter long because it’s made up of two (nonoverlapping) half-meter long parts, and that the half-meter long parts of the initial path have the lengths that they do because they are made of quarter-meter parts, which themselves have their lengths because of the lengths of still smaller parts, and so on.